

Solving Equations in One Variable

Using Graphing Calculators

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Solving Equations in One Variable Using Graphing Calculators

OBJECTIVE	USING TI-NSPIRE	USING TI-84
<p>Equivalent Expressions</p> <p>Complete the distributive property and verify the expressions are equivalent:</p> <p style="text-align: center;">$4(2x - 1)$</p>	<p>Using Tables</p> <p>-Start by opening a List & Spreadsheet window</p> <p>-Title column A: X</p> <p>-Title column B: first</p> <p>-Title column C: second</p> <p>Below the column title is a place to enter expressions.</p> <p>-Expression for column B: $4(2x-1)$</p> <p>You will be prompted to make a choice about using X, choose Variable Reference</p> <p>-Expression for column C: $8x-4$</p> <p>-Enter any value for x and IF the two expression are equivalent, columns B & C should be the same.</p> <p>-If expression values are not equivalent, make corrections in the functions cell and try again.</p>	<p>Using Tables</p> <p>-First enter the expressions in the equation editor, but the variable needs to be a column reference, we will use L₁ for our X column.</p> <p>Let $Y_1 = 4(2*L_1 - 1)$</p> <p>Let $Y_2 = 8*L_1 - 4$</p> <p>-Use STAT, EDIT to get to the tables window</p> <p>-In the L₁ column, enter one value</p> <p>-Move to the right and to the top of L₂ column</p> <p>-Enter "Y₁"</p> <p>-Move to the right and to the top of L₃ column</p> <p>-Enter "Y₂"</p> <p>Enter any other value in L₁, the expression columns should have equal values. If necessary, edit the expressions in the equation editor until you find them to be equivalent.</p>

Equivalent Expressions

Complete the distributive property and verify the expressions are equivalent:

$$4(2x - 1)$$

Using Graphs

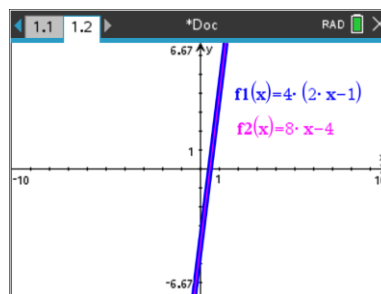
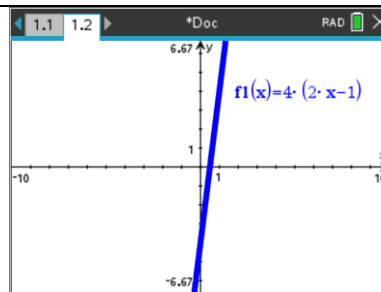
-Start in a graphing window

-Graph the original expression as the first function

-I would change the attributes to be a thicker line.

-Graph the equivalent expression as the second function. The new line should be on top of the original line.

-If lines are not coincident (concurrent), make corrections and try again.



Using Graphs

-First enter the expressions in the equation editor

$$\text{Let } Y_1 = 4(2x - 1)$$

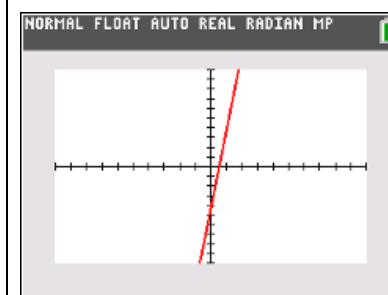
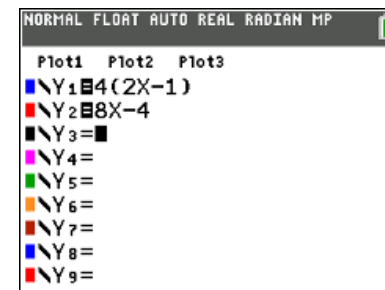
$$\text{Let } Y_2 = 8x - 4$$

-Press the GRAPH button below the screen and watch the graphs appear.

-If the expressions are equivalent, the graphs will be drawn in the same location (coincident lines)

-If the graphs show two different lines, then the expressions are not equivalent and need to be changed in the equation editor.

-Press the GRAPH button to see the changes.



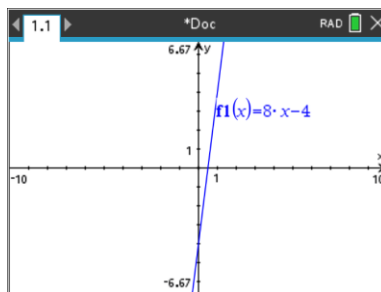
Solving Equations with Variables on One Side

Solve: $8x - 4 = 52$

Take the opportunity to have students look at the pattern in the numbers and discuss values where you see zeros

Using Tables

- Start by opening a graphing window and entering the variable expression as the first function
- Add a new page and make it a Lists & Spreadsheet
- Change the window to a Function Table and choose f1
- You can scroll down (or up) to view table values
- You are looking for which x value produces 52 for the function value
- You could use the Lists & Spreadsheet window by placing the variable expression in the function cell. This will allow you to choose any x value and view the calculated output.



X	f1(x):= 8*x-4
1.	4.
2.	12.
3.	20.
4.	28.
5.	36.

X	f1(x):= 8*x-4
3.	20.
4.	28.
5.	36.
6.	44.
7.	52.

A x	B first	C	D
=	=8*x-4		
4	4	28	
5	5	36	
6	6	44	
7	7	52	
8			

Using a Table

- First enter the expressions in the equation editor
Let $Y_1 = 8x - 4$
- Press ys to get to the function tables. The tables will already be complete.
- You can scroll down (or up) to view table values
- You are looking for which x value produces 52 for the function value

Plot1	Plot2	Plot3
$Y_1 = 8X - 4$		
$Y_2 =$		
$Y_3 =$		
$Y_4 =$		
$Y_5 =$		
$Y_6 =$		
$Y_7 =$		
$Y_8 =$		
$Y_9 =$		

X	Y1			
-1	-12			
0	-4			
1	4			
2	12			
3	20			
4	28			
5	36			
6	44			
7	52			
8	60			
9	68			

X = -1

Solving Equations with Variables on One Side

Solve: $8x - 4 = 52$

This is a teaching moment for students to see functions of a constant value produce horizontal lines

You could talk about the changes in the coordinates as they move the trace point. Recognizing patterns is a major focus.

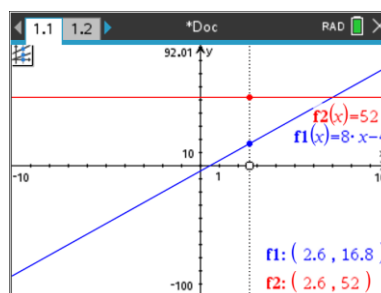
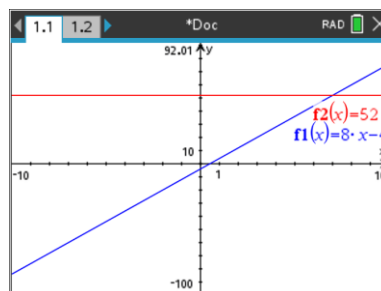
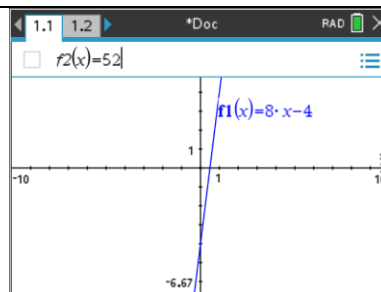
Why not bring up the topic of SYSTEMS at this point.

Using Graphing

- Return to the graphing window and enter a second function
- This will be a constant function $y = 52$

- You will need to adjust the viewing window.
- Time saving feature, use ZOOM FIT

- Use the TRACE ALL
- Set the TRACE STEP to be .1
- Arrow to the left and right to find the point where the coordinates are the same.



Using Graphing

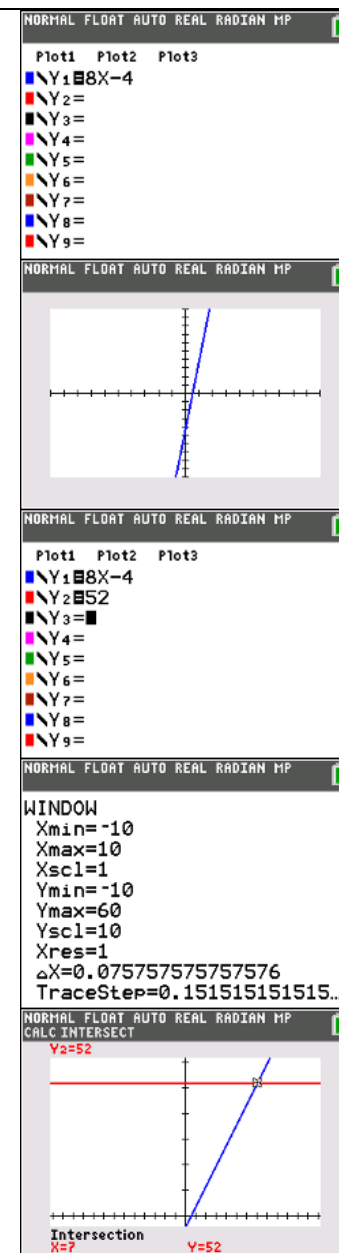
- First enter the expressions in the equation editor
- Let $Y_1 = 8x - 4$

- Press the GRAPH button below the screen and watch the graphs appear.

- Go back to the equation editor and enter the constant.

- You will need to adjust the viewing window; these are just a suggestion.

- Use yr to find the option for Intersection
- You will see the graph and be prompted to make choices, to find the x value of the intersection point.



Solving Equations with Variables on Both Sides

Solve:
 $15x+3=2(9+6x)$

Take the opportunity to have students look at the pattern in the numbers and discuss values where you see zeros.

Using Tables

- Start with a Lists & Spreadsheet
- Title column A: X
- Title column B: first
- Title column C: second
- Title column D: difference
- Below the column title is a place to enter expressions.
- Expression for column B: $15x + 3$

You will be prompted to make a choice about using X, choose **Variable Reference**

- Expression for column C: $2(9 + 6x)$
- Expression for column D: **first-second**

- Enter any value for x.
- You are looking for the X value that makes the two expressions equivalent, where columns B & C should be the same.
- If expression values are not equivalent, choose a different x.
- You should be observing if the difference in values is approaching zero, or not, to determine your next choice for X.

A	x	B first	C second	D difference...
1				
2				
3				
4				
5				

A	x	B first	C second	D difference...
1	1	18	30	-12
2	0	3	18	-15
3	4	63	66	-3
4	5	78	78	0
5				

A	x	B first	C second	D difference...
1	1	18	30	-12
2	0	3	18	-15
3	4	63	66	-3
4	5	78	78	0
5				

Using Tables

- First enter the expressions in the equation editor
 Let $Y_1 = 15x + 3$
 Let $Y_2 = 2(9 + 6x)$
 AND
 Let $Y_3 = Y_1 - Y_2$

- Then, go to the Table view and the values are filled in.

- Scroll up or down to see which x value produces the same value for the two expressions.
- Paying attention to the last column which is showing the difference between the expressions. The value should be zero.

X	Y1	Y2	Y3
-1	-12	6	-18
0	3	18	-15
1	18	30	-12
2	33	42	-9
3	48	54	-6
4	63	66	-3
5	78	78	0
6	93	90	3
7	108	102	6
8	123	114	9
9	138	126	12

X	Y1	Y2	Y3
-1	-12	6	-18
0	3	18	-15
1	18	30	-12
2	33	42	-9
3	48	54	-6
4	63	66	-3
5	78	78	0
6	93	90	3
7	108	102	6
8	123	114	9
9	138	126	12

Solving Equations with Variables on Both Sides

Solve:
 $15x+3=2(9+6x)$

You could talk about the changes in the coordinates as they move the trace point. Recognizing patterns is a major focus.

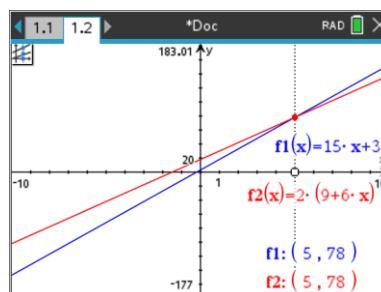
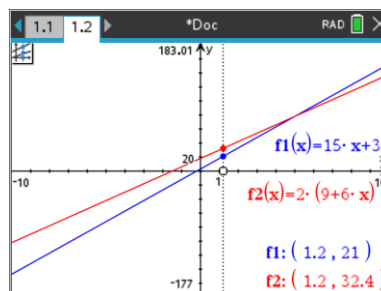
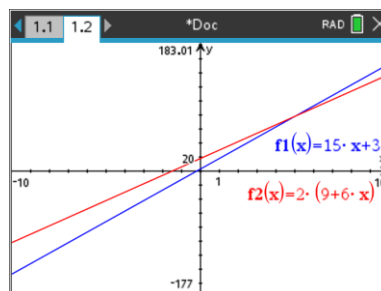
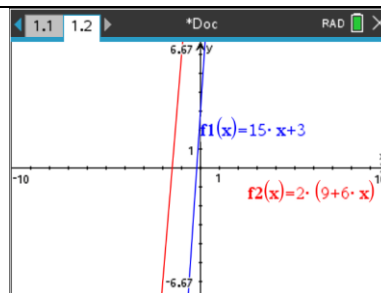
Of course, you can talk about the topic of SYSTEMS at this point.

Using Graphs

- Open a graphing window and enter the left expression as the first function
- Enter the right expression as the second function

- You may need to adjust the viewing window.
- Time saving feature, use ZOOM FIT

- Use the TRACE ALL
- Set the TRACE STEP to be .1
- Arrow to the left and right to find the point where the coordinates are the same.



Using Graphs

- First enter the expressions in the equation editor
 Let $Y_1 = 15x + 3$
 Let $Y_2 = 2(9 + 6x)$

- Press the Graph button and watch the graphs appear.
- You may need to change window settings
- Choose Zoom Fit to save time.

- Use yr to find the option for Intersection
- You will see the graph and be prompted to make choices, to find the x value of the intersection point.

